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- 1. Cover page,
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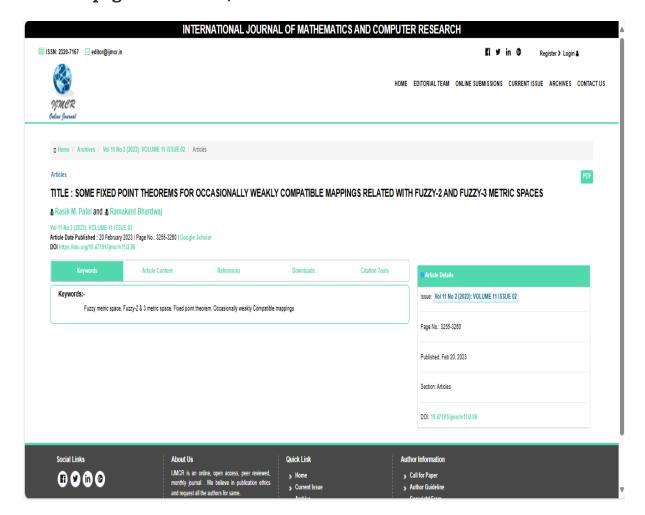


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# Some Fixed Point Theorems for Occasionally Weakly Compatible Mappings Related with Fuzzy-2 and Fuzzy-3 Metric spaces

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ARTICLE INFO	ABSTRACT
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#### I. INTRODUCTION

Impact of fixed point theory in different branches of mathematics and its applications is immense. The first result on fixed points for contractive type mapping was the much celebrated Banach's contraction principle by S. Banach [19] in 1922. In the general setting of complete metric space, this theorem runs as the follows, Theorem 1.1 (Banach's contraction principle) Let (X, d) be a complete metric space, c∈ (0, 1) and f:  $X \rightarrow X$  be a mapping such that for each  $x, y \in$ X, d  $(fx, fy) \le c d(x, y)$ . Then f has a unique fixed point  $a \in X$ , such that for each  $x \in X$ ,  $\lim_{n \to \infty} f^n x = a$ . After the classical result, R.Kannan [16] gave a subsequently new contractive mapping to prove the fixed point theorem. Since then a number of mathematicians have been worked on fixed point theory dealing with mappings satisfying various type of contractive conditions. In 2002, A. Branciari [1] analyzed the existence of fixed point for mapping f defined on a complete metric space (X, d) satisfying a general contractive condition of integral type.

Theorem 1.2 (A.Branciari) Let (X,d) be a complete metric space,  $c \in (0,1)$  and let  $f: X \to X$  be a mapping such that for each  $x,y \in X$ ,  $\int_0^{a(f \times f y)} \varphi(t) dt \leq c \int_0^{a(x \times y)} \varphi(t) dt$ . Where  $\varphi \colon [0,+\infty) \to [0,+\infty)$  is a Lebesgue integrable mapping which is summable on each compact subset of  $[0,+\infty)$ , non negative, and such that for each  $\varepsilon > 0$ ,  $\int_0^{\varepsilon} \varphi(t) dt$ , then f has a unique fixed point  $a \in X$ 

such that for each  $x \in X$ ,  $\lim_{n \to \infty} f^n x = a$  After the paper of Branciari, a lot of a research works have been carried out on generalizing contractive conditions of integral type for a different contractive mapping satisfying various known properties. A fine work has been done by Rhoades [3] extending the result of Branciari by replacing the condition by the

following 
$$\int_{0}^{d(J \times f y)} \varphi(t) dt \leq \int_{0}^{max \left\{ d(x,y), d(x,f x), d(y,f y), \frac{d(x,f y) + d(y,f x)}{2} \right\}} \varphi(t) dt$$

The aim of this paper is to generalize some mixed type of contractive conditions to the mapping and then a pair of mappings, satisfying a general contractive mapping such as R. Kannan type [16], S.K. Chattrerjee type [20], T. Zamfirescu type [25], Schweizer and A.Sklar [21]etc.

The concept of Fuzzy sets was introduced initially by Zadeh [27]. Since then, to use this concept in topology and analysis many authors have expansively developed the theory of fuzzy sets. Both George and Veermani [4], Kramosil [8] modified the notion of fuzzy metric spaces with the help of continuous t-norms. Many researchers have obtained common fixed point theorems for mappings satisfying different types of commutativity conditions. Vasuki [17] proved fixed point theorems for R-weakly commutating mappings. R.P. Pant and Jha [13, 14, 15] introduced the new concept reciprocally continuous mappings and established

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